

مقدمه

محوريا شافت:

عضوي چرخشي يا ثابت، ومعمولا با مقطع دايره اي براي انتقال توان یا حرکت از دستگاه محرک، نظیر یک موتور الکتریکی، به یک مصر ف كننده

بر روی شافت معمولا چرخدنده، پولی و چرخ زنجیرنصب گردیده که انتقال حرکت چرخشی و توان را توسط دنده های درگیر، تسمه

وزنجیر میسر می سازند



Photo courtesy Emerson Power Transmission Corp

اصول طراحي شافت

- Material Selection
- Geometric Layout
- Stress and strength
 - Static strength
 - Fatigue strength
- Deflection and rigidity
 - Bending deflection
 - Torsional deflection
 - Slope at bearings and shaft-supported elements
 - Shear deflection due to transverse loading of short shafts
- Vibration due to natural frequency



ملاحظاتي برجنس محورها

- Deflection primarily controlled by geometry, not material
- Stress controlled by geometry, not material
- Strength controlled by material property



جنس محورها

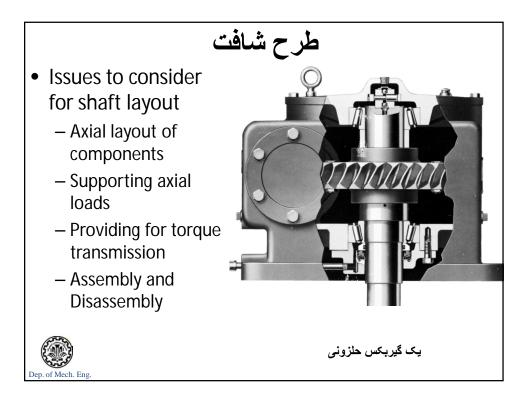
- Shafts are commonly made from low carbon,
 CD or HR steel, such as ANSI 1020–1050 steels.
- Fatigue properties don't usually benefit much from high alloy content and heat treatment.
- Surface hardening usually only used when the shaft is being used as a bearing surface.



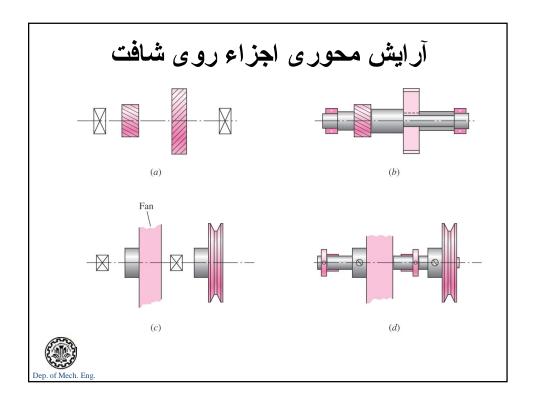
جنس محورها

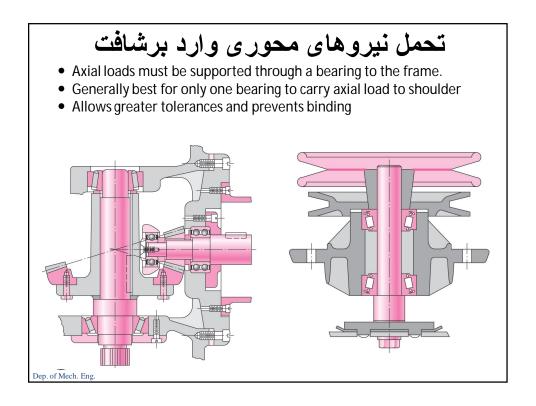
- Cold drawn steel typical for *d* < 3 in.
- HR steel common for larger sizes. Should be machined all over.
- Low production quantities
 - Lathe machining is typical
 - Minimum material removal may be design goal
- High production quantities
 - Forming or casting is common
 - Minimum material may be design goal







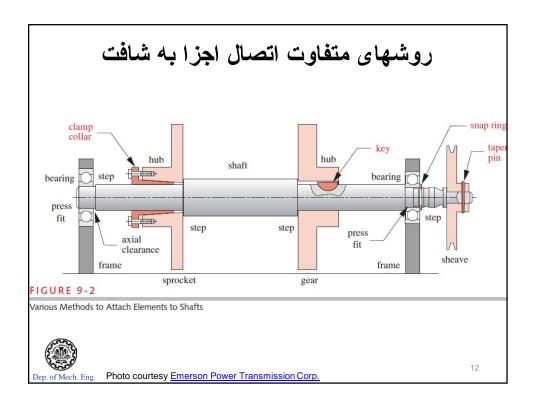


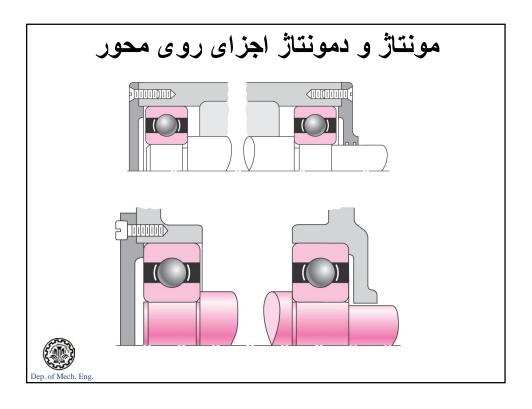


روشهای انتقال گشتاوربه محور

- Common means of transferring torque to shaft
 - Keys
 - Splines
 - Setscrews
 - Pins
 - Press or shrink fits
 - Tapered fits
- Keys are one of the most effective
 - Slip fit of component onto shaft for easy assembly
 - Can design key to be weakest link to fail in case of overload









نکات مهم در طراحی محورها

- طراحی کوتاه محور تا حد امکان
- نزدیکی یاتاقانها به محل های اعمال بار (به منظور کاهش ممان خمشی و خیزشافت، افزایش سرعت بحرانی)
 - دور نگه داشتن تتش افزاها از محل های با تتش بالا
 - ایجاد قوس های ملایم در گوشه یله ها
 - افز ایش کیفیت سطح محور
- در نظر گرفتن عملیات احتمالی محلی سطح نظیر نورد سرد یا شات سنینگ
 - استفاده از شافت توخالی در صورت مهم بودن شاخص وزن



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روند طراحی یک محور با بار ثابت

- 1. تعیین سرعت چرخشی شافت
- 2. تعین توان یا تورکی که توسط شافت انتقال می یابد
- تعیین ابعاد اجزا انتقال قدرت ودیگر اجزایی که روی شافت سوار میشوند
 - 4. تعیین موقعیت یاتاقانهای نگه دارنده شافت
- 5. ارائه طرح هندسی شافت با در نظر گرفتن اینکه هر جزء درکجا قرار میگیرد و انتقال قدرت چگونه منتقل میشود
 - 6. تعیین اندازه تورک در طول شافت
 - 7. تعیین نیروهای وارده بر شافت
 - 8. ترسیم نمودارهای نیروی برشی و ممان خنثی
 - 9. انتخاب جنس برای شافت و عملیات حرارتی احتمالی



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روند طراحی یک محور با بار ثابت

10.با در نظر گرفتن نوع بارگذاری (ملایم، شوکی، تکرارشونده، معکوس) تعیین تش طراحی

11. تحلیل و آنالیز همه نقاط بحرانی روی شافت و تعیین حداقل قطرهای قابل قبول به منظور اطمینان از طراحی ایمن

12. تعيين ابعادنهايي شافت



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ملاحظات خيز شافت

- Deflection analysis at a single point of interest requires complete geometry information for the entire shaft.
- For this reason, a common approach is to size critical locations for stress, then fill in reasonable size estimates for other locations, then perform deflection analysis.
- Deflection of the shaft, both linear and angular, should be checked at gears and bearings.



Mohsen Badrossamay

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ملاحظات خيز شافت

 Allowable deflections at components will depend on the component manufacturer's specifications.

Table 7-2	Slopes				
Typical Maximum	Tapered roller	0.0005-0.0012 rad			
Ranges for Slopes and	Cylindrical roller	0.0008-0.0012 rad			
Transverse Deflections	Deep-groove ball	0.001-0.003 rad			
	Spherical ball	0.026-0.052 rad			
	Self-align ball	0.026-0.052 rad			
	Uncrowned spur gear	< 0.0005 rad			
	Transverse Deflections				
	Spur gears with $P < 10$ teeth/in	0.010 in			
	Spur gears with $11 < P < 19$	0.005 in			
	Spur gears with $20 < P < 50$	0.003 in			
ey's Mechanical Engineering Design Mech. Eng.					

ملاحظات خيز شافت

- Deflection analysis is straightforward, but lengthy and tedious to carry out manually.
- Each point of interest requires entirely new deflection analysis.
- Consequently, shaft deflection analysis is almost always done with the assistance of software.
- Options include specialized shaft software, general beam deflection software, and finite element analysis software.



Example 7-3

This example problem is part of a larger case study. See Chap. 18 for the full context.

In Ex. 7-2, a preliminary shaft geometry was obtained on the basis of design for stress. The resulting shaft is shown in Fig. 7-10, with proposed diameters of

$$D_1 = D_7 = 1$$
 in
 $D_2 = D_6 = 1.4$ in
 $D_3 = D_5 = 1.625$ in

Check that the deflections and slopes at the gears and bearings are acceptable. If necessary, propose changes in the geometry to resolve any problems.

 $D_4 = 2.0 \text{ in}$

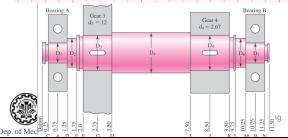


Fig. 7-10

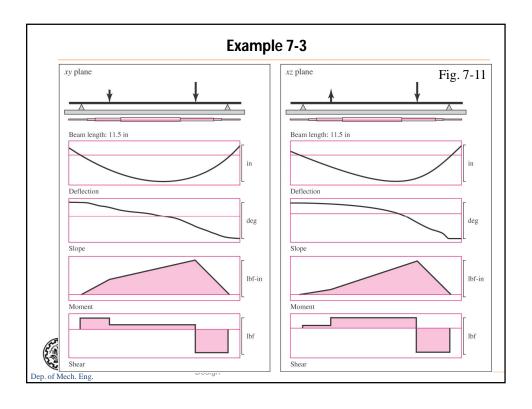
Example 7-3

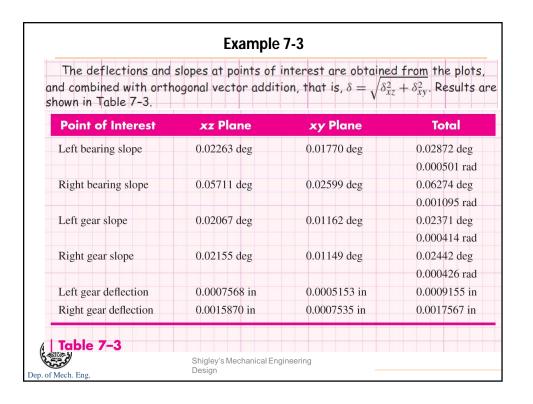
Solution

A simple planar beam analysis program will be used. By modeling the shaft twice, with loads in two orthogonal planes, and combining the results, the shaft deflections can readily be obtained. For both planes, the material is selected (steel with $E=30~\rm Mpsi$), the shaft lengths and diameters are entered, and the bearing locations are specified. Local details like grooves and keyways are ignored, as they will have insignificant effect on the deflections. Then the tangential gear forces are entered in the horizontal xz plane model, and the radial gear forces are entered in the vertical xy plane model. The software can calculate the bearing reaction forces, and numerically integrate to generate plots for shear, moment, slope, and deflection, as shown in Fig. 7-11.



Shigley's Mechanical Engineering Design





Example 7-3

Whether these values are acceptable will depend on the specific bearings and gears selected, as well as the level of performance expected. According to the guidelines in Table 7-2, all of the bearing slopes are well below typical limits for ball bearings. The right bearing slope is within the typical range for cylindrical bearings. Since the load on the right bearing is relatively high, a cylindrical bearing might be used. This constraint should be checked against the specific bearing specifications once the bearing is selected.

The gear slopes and deflections more than satisfy the limits recommended in Table 7-2. It is recommended to proceed with the design, with an awareness that changes that reduce rigidity should warrant another deflection check.



Shigley's Mechanical Engineering Design

سرعت بحرانی محور

- A shaft with mass has a critical speed at which its deflections become unstable.
- Components attached to the shaft have an even lower critical speed than the shaft.
- Designers should ensure that the lowest critical speed is at least twice the operating speed.



سرعت بحرانی محور

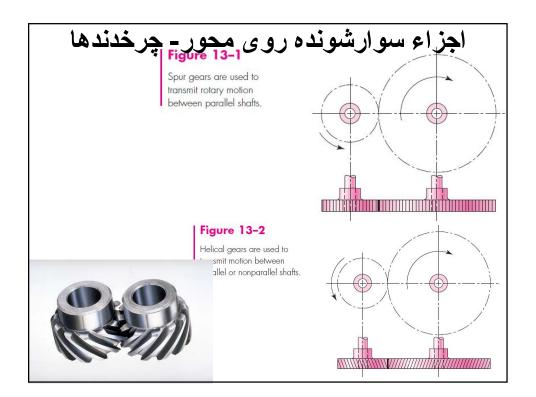
 For a simply supported shaft of uniform diameter, the first critical speed is

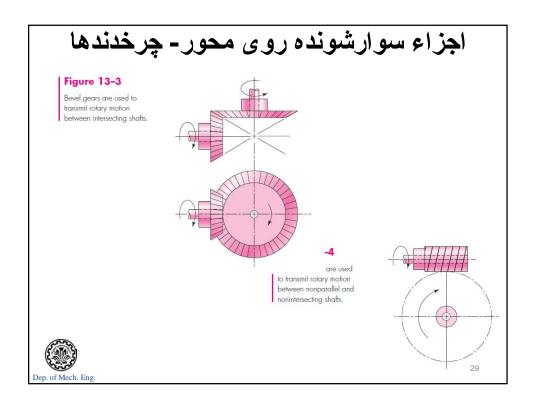
$$\omega_1 = \left(\frac{\pi}{l}\right)^2 \sqrt{\frac{EI}{m}} = \left(\frac{\pi}{l}\right)^2 \sqrt{\frac{gEI}{A\gamma}} \tag{7-22}$$

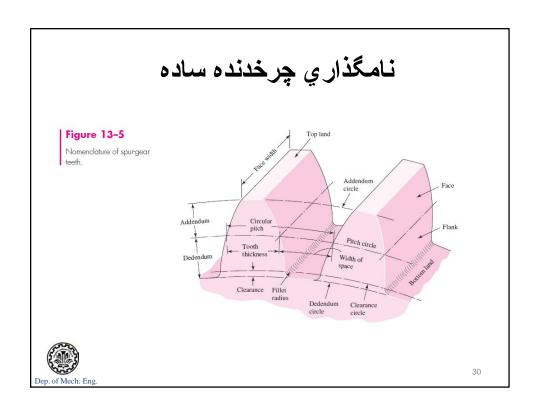
 For an ensemble of attachments, Rayleigh's method for lumped masses gives

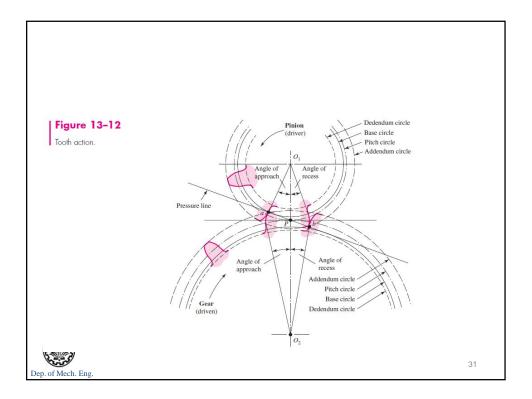
$$\omega_1 = \sqrt{\frac{g \sum w_i y_i}{\sum w_i y_i^2}} \tag{7-23}$$

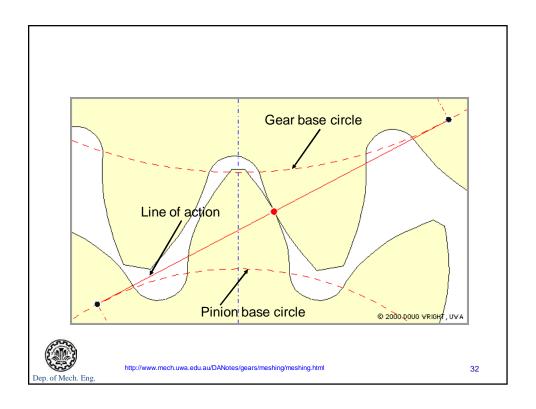


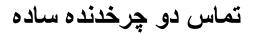


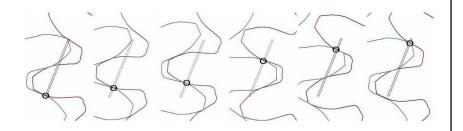










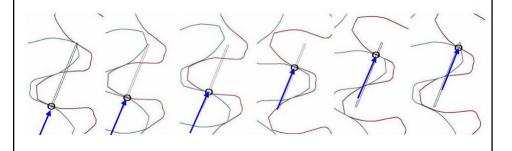


نقطه تماس همواره بر روی خط عمل قرار دارد.



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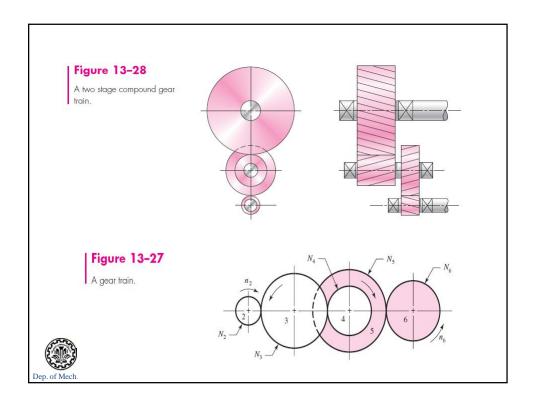
جهت نیرو در تماس بین دو چرخدنده ساده

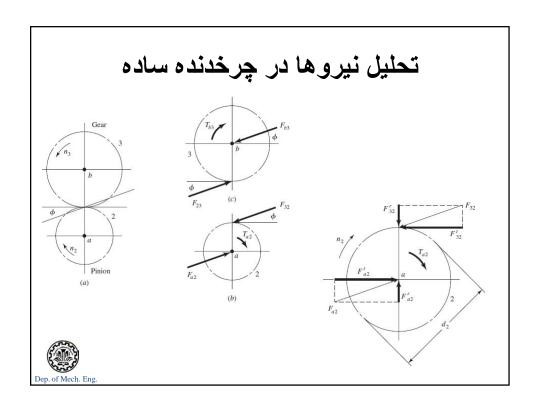


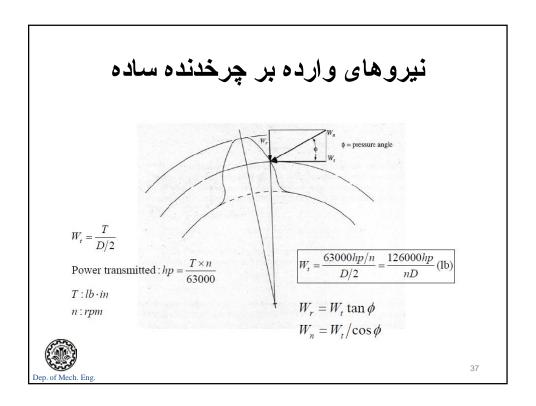
راستای اعمال نیرو در جهت خط عمل قرار دارد.

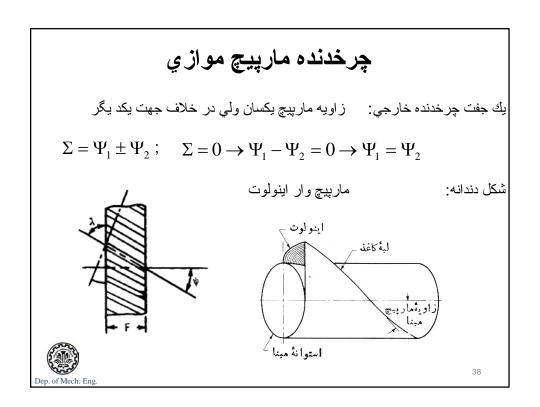


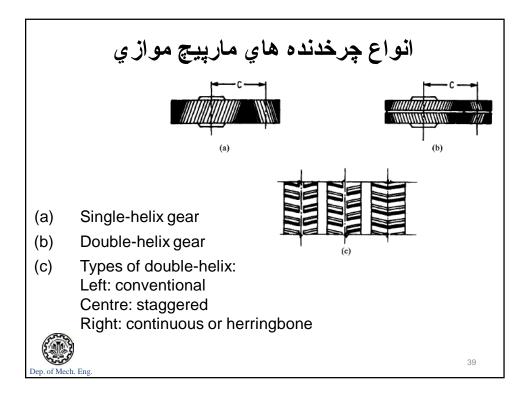
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چرخدنده های جناقی

 To avoid axial thrust, two helical gears of opposite hand can be mounted side by side, to cancel resulting thrust forces



 Herringbone gears are mostly used on heavy machinery.





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چرخدنده مارپیچ موازي--مشخصه ها

خط - نقطه – خط:

نحوه تماس:

در گیر ی تدر یجی دندانه ها

■ انتقال آرام بار

■ تو انایی انتقال بار های سنگین در سر عتهای بالا

■ اهمیت کم نسبت تماس

ایجاد مولفه نیرویی محوری (علاوه بر شعاعی) ز اويه مارېيچ:

با افزایش ψ ایجاد سروصدا کاهش می بابد (انتقال قدرت

یکنواخت تر)

با افزایش ψ نیروی محوری افزایش می یابد عموما 15, 23, 30و °45



برش A-A.

نامگذاری چرخدنده های مارپیچ

گام دایره ای: • گام دایره ای عرضی (گام دایره ای) - Pt

■ گام دایر ه ای عمو دی - Pn

■ گام دایره ای عرضی (گام محوری) - Px

 ■ مدول عرضى (مدول)- m مدول:

■ مدول عمودی - mn

 $P_n = P_t \cos \Psi$

 $P_{t} = \pi \cdot m$

 $P_x = \frac{P_t}{\tan \Psi}$

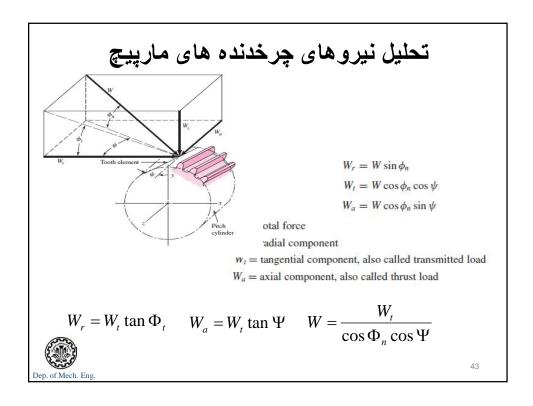
 $P_n = \pi \cdot m_n$

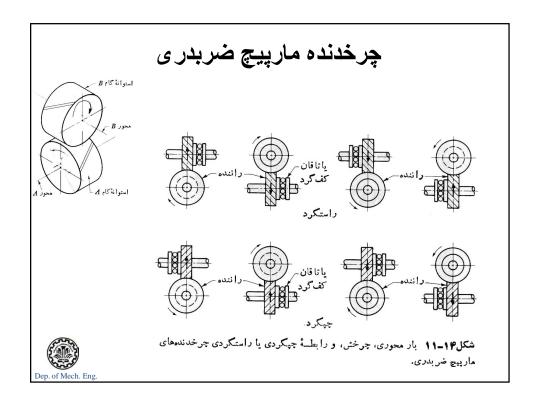
 $m_n = m \cos \Psi$

 $\cos\Psi = \frac{\tan\Phi_n}{\tan\Phi_n}$

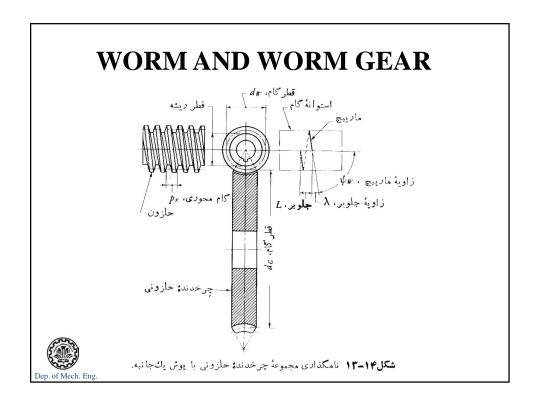
شکل۳-۱۳ نامکداری چرخدندههای مارپیج.

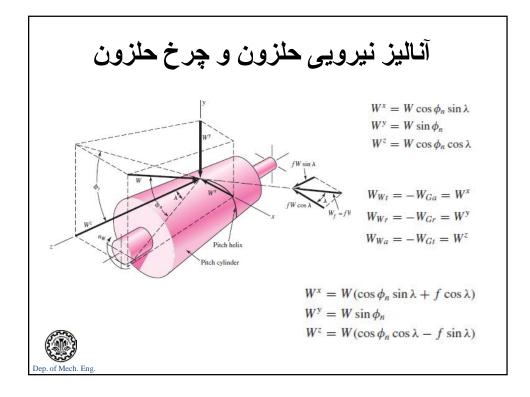
42







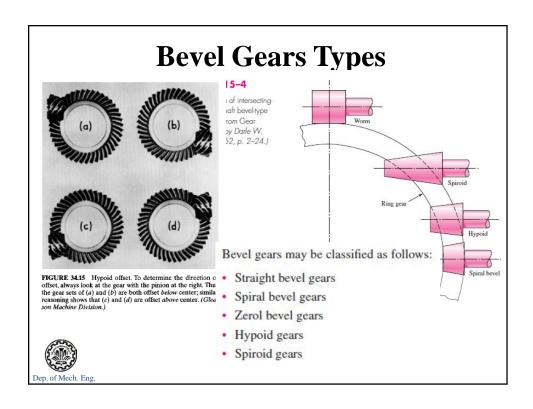




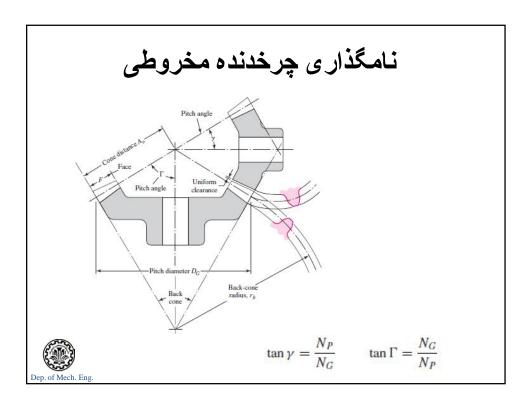
Bevel gears

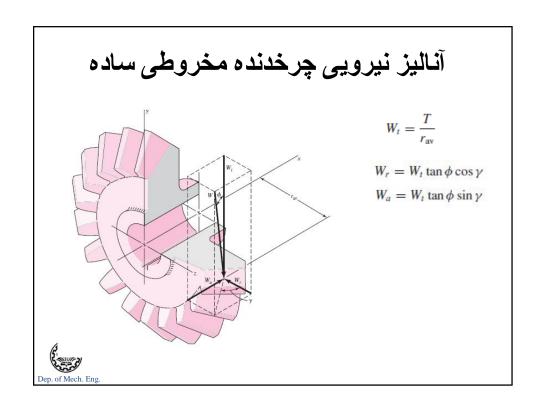
- **Bevel gears** are useful when the direction of a shaft's rotation needs to be changed
- They are usually mounted on shafts that are 90 degrees apart, but can be designed to work at other angles as well
- The teeth on bevel gears can be straight, spiral or hypoid
- locomotives, marine applications, automobiles, printing presses, cooling towers, power plants, steel plants, railway track inspection machines, etc.

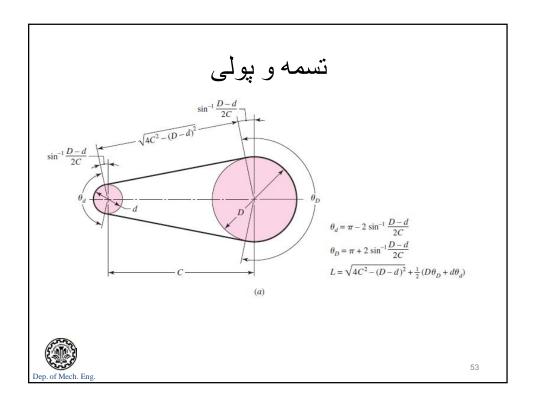


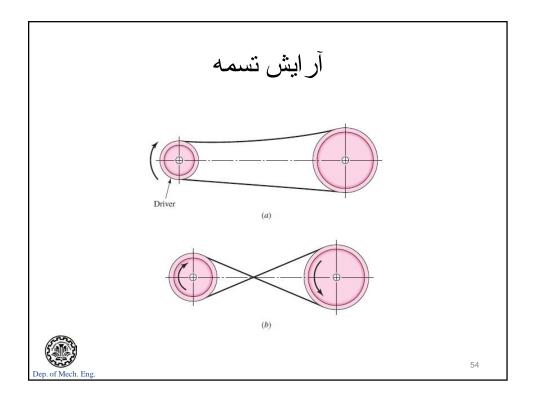


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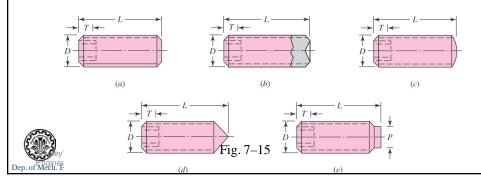




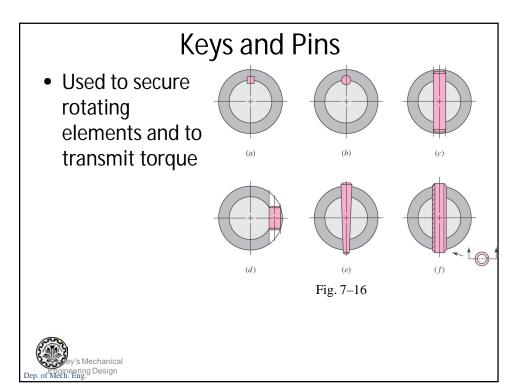


Setscrews

- Setscrews resist axial and rotational motion
- They apply a compressive force to create friction
- The tip of the set screw may also provide a slight penetration
- Various tips are available



Setscrews T	Table 7–4 Sypical Holding Power Force) for Socket	Size,	Seating Torque, Ibf•in	Holding Power, Ibf
1.	etscrews*	#0	1.0	50
~	ource: Unbrako Division, SPS	#1	1.8	65
	echnologies, Jenkintown, Pa.	#2	1.8	85
• Desistance to evial man	tion of collar	#3	5	120
 Resistance to axial mo 	tion of collar	#4	5	160
or hub relative to shaf	t is called	#5	10	200
holding nower		#6 #8	10 20	250 385
holding power		#8 #10	20 36	540
• Typical values listed in	Table 7-4	$\frac{1}{4}$	87	1000
apply to axial and torsi	ional	$\frac{5}{16}$	165	1500
113	oriai	$\frac{3}{8}$	290	2000
resistance		$\frac{7}{16}$	430	2500
• Tunical factors of cofet		$\frac{1}{2}$	620	3000
 Typical factors of safet 	y are 1.5 to	9 16	620	3500
2.0 for static, and 4 to	8 for	5 8	1325	4000
•		$\frac{3}{4}$	2400	5000
dynamic loads		7/8	5200	6000
• gth should be abou	it half the	1	7200	7000



Tapered Pins

- Taper pins are sized by diameter at large end
- Small end diameter is

$$d = D - 0.0208L$$

(7 - 35)

• Table 7–5 shows some standard sizes in inches

	Comm	ercial	ıl Precision	
Size	Maximum	Minimum	Maximum	Minimum
4/0	0.1103	0.1083	0.1100	0.1090
2/0	0.1423	0.1403	0.1420	0.1410
0	0.1573	0.1553	0.1570	0.1560
2	0.1943	0.1923	0.1940	0.1930
4	0.2513	0.2493	0.2510	0.2500
6	0.3423	0.3403	0.3420	0.3410
8	0.4933	0.4913	0.4930	0.4920
Engineering D	esign	Table 7–5		

		Keys			
Keys come in	Shaft Over	Diameter To (Incl.)	Key w	Size h	Keyway Depth
standard	$\frac{\frac{5}{16}}{\frac{7}{16}}$	$\frac{\frac{7}{16}}{\frac{9}{16}}$	$\frac{\frac{3}{32}}{\frac{1}{8}}$	$\frac{\frac{3}{32}}{\frac{3}{32}}$	$\frac{\frac{3}{64}}{\frac{3}{64}}$
square and			$\frac{1}{8}$ $\frac{3}{16}$	$\frac{1}{8}$	$\frac{1}{16}$
rectangular	9 16	7/8	$\frac{3}{16}$	$\frac{\frac{1}{8}}{\frac{3}{16}}$	$\frac{1}{16}$ $\frac{3}{32}$
sizes	$\frac{7}{8}$	$1\frac{1}{4}$	$\frac{\frac{1}{4}}{\frac{1}{4}}$	$\frac{3}{16}$ $\frac{1}{4}$	$\frac{\frac{3}{32}}{\frac{1}{8}}$
 Shaft diameter 	$1\frac{1}{4}$	$1\frac{3}{8}$	5 16 5 16	$\frac{\frac{1}{4}}{\frac{5}{16}}$	$\frac{\frac{1}{8}}{\frac{5}{32}}$
determines key	$1\frac{3}{8}$	$1\frac{3}{4}$	3 8 3 8	$\frac{1}{4}$ $\frac{3}{8}$	$ \begin{array}{r} 32 \\ \frac{1}{8} \\ \frac{3}{16} \end{array} $
size	$1\frac{3}{4}$	$2\frac{1}{4}$	$\frac{8}{2}$	$\frac{3}{8}$	$\frac{3}{16}$
	$2\frac{1}{4}$	$2\frac{3}{4}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{5}{8}$ $\frac{5}{8}$	$\frac{\frac{1}{2}}{\frac{7}{16}}$	$\frac{1}{4}$ $\frac{7}{32}$
	$2\frac{3}{4}$	$3\frac{1}{4}$		$\frac{5}{8}$ $\frac{1}{2}$	$ \begin{array}{r} 5\\ 16\\ \frac{1}{4} \end{array} $
ey's Mechanical		-	$\frac{3}{4}$	3 4	3/8
Dep. of Mech. Eng. Table 7–6	i				

Keys

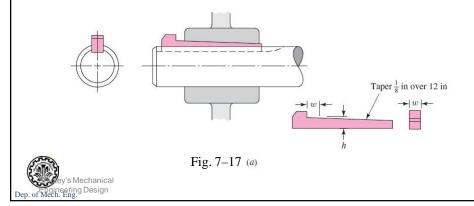
- Failure of keys is by either direct shear or bearing stress
- Key length is designed to provide desired factor of safety
- Factor of safety should not be excessive, so the inexpensive key is the weak link
- Key length is limited to hub length
- Key length should not exceed 1.5 times shaft diameter to avoid problems from twisting
- Multiple keys may be used to carry greater torque, typically oriented 90° from one another
- Stock key material is typically low carbon cold-rolled steel, with dimensions slightly under the nominal

imensions to easily fit end-milled keyway

Dep. of Mech. Eng

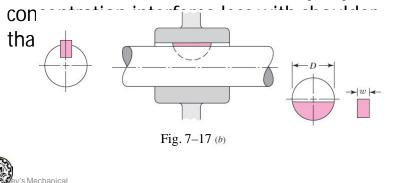
Gib-head Key

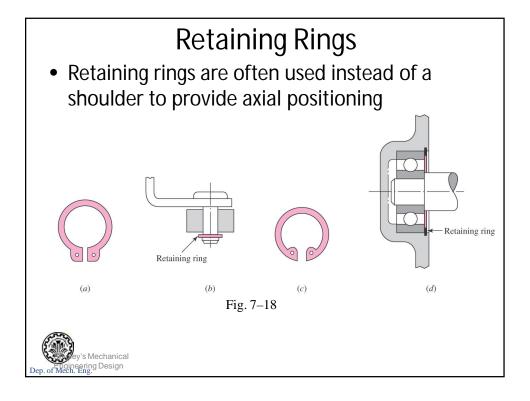
- Gib-head key is tapered so that when firmly driven it prevents axial motion
- Head makes removal easy
- · Projection of head may be hazardous



Woodruff Key

- Woodruff keys have deeper penetration
- Useful for smaller shafts to prevent key from rolling
- When used near a shoulder, the keyway stress





Retaining Rings

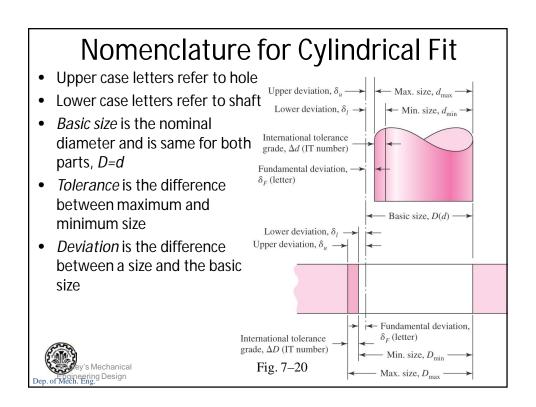
- Retaining ring must seat well in bottom of groove to support axial loads against the sides of the groove.
- This requires sharp radius in bottom of groove.
- Stress concentrations for flat-bottomed grooves are available in Table A–15–16 and A–15–17.
- Typical stress concentration factors are high, around 5 for bending and axial, and 3 for torsion



Limits and Fits

- Shaft diameters need to be sized to "fit" the shaft components (e.g. gears, bearings, etc.)
- Need ease of assembly
- Need minimum slop
- May need to transmit torque through press fit
- Shaft design requires only nominal shaft diameters
- Precise dimensions, including tolerances, are necessary to finalize design





Description of Preferred Fits (Clearance)				
Type of Fit	Description	Symbol		
Clearance	Loose running fit: for wide commercial tolerances or allowances on external members	H11/c11		
	Free running fit: not for use where accuracy is essential, but good for large temperature variations, high running speeds, or heavy journal pressures	H9/d9		
	Close running fit: for running on accurate machines and for accurate location at moderate speeds and journal pressures	H8/ſ7		
	Sliding fit: where parts are not intended to run freely, but must move and turn freely and locate accurately	H7/g6		
	Locational clearance fit: provides snug fit for location of stationary parts, but can be freely assembled and disassembled	H7/h6		
	Table 7–9			
Dep. of Mech. Eng.	Shigley's Mechanical Engineering Design			

Description of Preferred Fits (Transition & Interference)					
Type of Fit	Description	Symbol			
Transition	Locational transition fit: for accurate location, a compromise between clearance and interference	H7/k6			
	Locational transition fit: for more accurate location where greater interference is permissible	H7/n6			
Interference	Locational interference fit: for parts requiring rigidity and alignment with prime accuracy of location but without special bore pressure requirements	H7/p6			
	Medium drive fit: for ordinary steel parts or shrink fits on light sections, the tightest fit usable with cast iron	H7/s6			
	Force fit: suitable for parts that can be highly stressed or for shrink fits where the heavy pressing forces required are impractical	H7/u6			
	Table 7–9				
Dep. of Mech. Eng.	Shigley's Mechanical Engineering Design				

Shaft Design for Stress

- Stresses are only evaluated at critical locations
- Critical locations are usually
 - On the outer surface
 - Where the bending moment is large
 - Where the torque is present
 - Where stress concentrations exist

